## Section 2.4: Permutations When Objects are Identical

A permutation of 'n' elements taken 'n' at a time ( ${ }_{n} P_{n}$ or $n!$ ) is affected if one or more elements in the set are IDENTICAL.

## For example,

If a set of 3 marbles consists of 2 identical green marbles and 1 blue marble, the set $\{G 1, G 2, B\}$ is identical to $\{G 2, G 1, B\}$. This configuration is counted as two different arrangements instead of one.

Therefore, it must be removed from the total count by dividing out repetitions ( $\frac{3!}{2!}$ )

In general,
The number of permutations of ' $n$ ' objects containing 'a' identical objects of one kind and 'b' identical objects of another kind and so on is:

$$
\frac{n!}{a!b!\ldots}
$$

Dividing $n$ ! by $a$ ! and b! eliminates arrangements that are the same and that would otherwise be counted multiple times.

## Example 1:

If there are 9 different cookies (4 chocolate chip, 3 oatmeal and 2 raisin), in how many different orders can you eat all of them if you eat one at a time?

## Example 2:

How many different ways can you arrange the letters in the word MATHEMATICS?

Example 3: (ex. 2, p. 101)
How many ways can the letters in CANADA be arranged, if the first letter must be N and the last letter must be C ?

Example 4: (ex. 3, p. 102)
Julie's home is three blocks north and five blocks west of her school. How many routes can Julie take from home to school if she always travels either south or east?


## Example 5:

Determine the number of routes there are to get from point $A$ to point $B$, if you travel only south or east?



## Practice Questions: <br> p.104-107, \#4,5,6bd,7ab,9a,10,(11ab),12,15ab,16,17ab

