Name:\_\_\_\_\_

## **Multiple Choice**

- **1.** Which of the following is an exponential function?
  - **A.**  $f(x) = x^2$  **B.**  $g(x) = (-1)^x$  **C.**  $h(x) = 17^x$ **D.**  $j(x) = 2^3 - x$
- **2.** Match the following graph with its function.



**A.** 
$$y = 3(0.5)^{x}$$
  
**B.**  $y = 2(1.25)^{x}$   
**C.**  $y = 0.5(3)^{x}$   
**D.**  $y = 2(0.75)^{x}$ 

**3.** Match the following graph with its function.



**A.**  $y = 3(0.5)^{x}$  **B.**  $y = 2(1.25)^{x}$  **C.**  $y = 0.5(3)^{x}$ **D.**  $y = 2(0.75)^{x}$ 

**4.** Identify the range of the exponential function  $y = 10^x$ .

A.  $\{y \mid y < 0, y \in R\}$ B.  $\{y \mid y > 0, y \in R\}$ C.  $\{y \mid y \neq 0, y \in R\}$ D.  $\{y \mid y \in R\}$  5. Determine the *y*-intercept of the exponential function  $f(x) = 4\left(\frac{1}{2}\right)^n$ .

- **A.** 0
- **B.** 1
- **C.** 2 **D.** 4

6. Which option best describes the behaviour of the exponential function  $f(x) = 4\left(\frac{1}{2}\right)^n$ ?

- A. increasing because a > 1
- **B.** decreasing because 0 < a < 1
- **C.** increasing because b > 1
- **D.** decreasing because 0 < b < 1
- 7. Express  $\left(\sqrt{32}\right)^{2\pi}$  as a power with a base of 2.

  - **A.**  $2^{5x}$  **B.**  $2^{10x}$  **C.**  $2^{25x}$  **D.**  $2^{20x}$

8. Express  $\left(\frac{1}{27}\right)^{n+1}$  as a power with a base of 3.

- **A.** 3<sup>3x-3</sup> **B.** 3<sup>-3x-3</sup>
- C.  $3^{-3x+3}$
- **D.**  $3^{3x+3}$
- 9. Solve the following exponential equation by writing both sides with the same base.  $2(3)^{x} = 162$ 
  - **A.** x = 2**B.** *x* = 3 **C.** x = 4**D.** x = 5
- 10. Solve the following exponential equation by writing both sides with the same base.  $2^{3-z} = \frac{1}{32}$ 
  - **A.** *z* = 7 **B.** z = 8**C.** z = 9**D.** z = 10
- 11. The population of a specific bacteria growing in a Petri dish is modelled by the function

 $P(t) = 5000(2)^{\frac{t}{3}}$ , where P(t) represents the number of bacteria and t represents the time, in days, after the initial time. How long does it take for the population to double?

- **A.** 1 day
- **B.** 2 days
- C. 3 days
- **D.** 9 days

12. The following data set involves exponential growth. Determine the missing value from the table.

x	0	1	2	3	4	5	6
у	0.16	0.40	1.00	2.50		15.63	39.06

**A.** 6.25

**B.** 5.00

C. 7.50D. 8.75

13. Determine the equation of the exponential regression function for the data.

x	0	1	2	3	4	5
у	74.8	60.2	47.8	38.3	30.8	24.4

**A.**  $y = 75(0.8)^x$ 

**B.**  $y = 75(1.6)^x$ 

- **C.**  $y = 60(0.8)^x$
- **D.**  $y = 60(1.6)^x$

**14.** A scatter plot is drawn using a data set.



Identify the equation of the curve of best fit.

- **A.**  $y = 12(1.3)^{x}$  **B.**  $y = 12(0.3)^{x}$  **C.**  $y = 4(1.5)^{x}$ **D.**  $y = 4(0.5)^{x}$
- **15.** The equation of the exponential function that models a data set is  $y = 6.8(1.03)^x$ . Determine the range of this function.
  - A.  $\{y \mid y > 0, y \in R\}$ B.  $\{y \mid y \in R\}$ C.  $\{y \mid y > 6.8, y \in R\}$ D.  $\{y \mid y > 1.03, y \in R\}$
- 16. An investment can be modelled by the following growth function, where x represents the time in years:

 $y = 2500(1.018)^{x}$ . What was the principal invested?

A. \$1250B. \$2500C. \$18D. \$1018

**17.** An investment can be modelled by the following growth function, where *x* represents the time in years:

 $y = 2500(1.018)^{x}$ . What was the annual interest rate for the investment?

**A.** 25%

- **B.** 1.018%
- C. 18%D. 1.8%
- **18.** Eli invested \$1000 at 3%/a compounded quarterly.

Define an exponential growth function for this investment in the form  $A(n) = P(1 + i)^n$  where *n* represents the number of compounding periods.

**A.**  $A(n) = 1000(1.003)^n$  **B.**  $A(n) = 1000(1.0075)^n$  **C.**  $A(n) = 1000(1.03)^n$ **D.**  $A(n) = 4000(1.03)^n$ 

**19.** Denis recently spent \$1280 on a new laptop for his home business. He read that the depreciation rate for this model laptop is 25%.

How much money should Denis expect to sell his laptop for in three years?

- **A.** \$540
- **B.** \$960**C.** \$320
- **D.** \$740
- 20. Solve the following exponential equation by writing both sides with the same base.  $\sqrt{1000} = 10^{2a-1}$
- **21.** A research lab has a 12 mg sample of a radioactive substance. The amount of the substance, A(t), left in the sample can be modelled by the half-life function

$$A(t) = 12 \left(\frac{1}{2}\right)^{\frac{t}{85}}$$

where *t* represents the time, in days, after the initial time. How long does it take for the sample to reduce to one quarter its initial amount?

**22.** Determine whether the following data set involves exponential growth, exponential decay, or neither. Explain how you know.

x	1	2	3	4	5	6
у	5	15	45	135	405	1215

23. The fish population in Loon Lake is modelled by the equation  $P(t) = 2500(0.92)^t$  where P(t) represents the number of fish and t represents the time

where P(t) represents the number of fish and *t* represents the time, in years, since 2010. Estimate the fish population in 2030.

**24.** Complete the table of values for a \$350 investment earning 2.5%/a compounded monthly.

Time (months)	0	1	2	3
Value (\$)	350.00	350.73		

**25.** Nina invested \$3000 at 1.3%/a compounded weekly.

Define an exponential growth function for this investment in the form  $A(n) = P(1 + i)^n$ , where *n* represents the number of compounding periods.

26. A vehicle was purchased for \$15 000 in 2005. The book value of the vehicle can be modelled by the exponential function  $y = 15\ 000(0.82)^{x}$ 

where y represents the value in dollars and x represents the time, in years, after 2005.

a) How does the value of the vehicle change over time? Explain how you know.

**b**) Estimate the value of the vehicle in 2015. Show your work.

27. Use what you know about the exponential function  $y = \left(\frac{1}{2}\right)^x$  to predict the number of *x*-intercepts, the *y*-intercept, the end behaviour, increasing or decreasing, the domain, and the range of the

following functions:

- a)  $y = \left(\frac{1}{2}\right)^x$  b)  $y = 4(3)^x$
- **28.** Solve the equation and verify your answer by substitution. Show your work.  $6(8)^{5-\kappa} = 3072$
- **29.** Solve the equation and verify your answer by substitution. Show your work.  $8^{n+1} = 32^{n-1}$
- **30.** Thorium-227 has a half-life of 18.4 days. The remaining amount of a 50-mg sample of thorium-227 can be modelled by the equation

$$A(t) = 50 \left(\frac{1}{2}\right)^{\frac{t}{184}}$$

where A(t) is the amount of thorium-227 remaining, in milligrams, and *t* is the time in days. Determine the amount of thorium-227 remaining after 10 days, to the nearest milligram. Show your work.

- 31. 234 bi-weekly payments are required to pay off a loan. How many years does this represent?
- **32**. A student repaid a total of \$2393.36 for a loan including the principal and interest. If the interest rate was 6% compounded monthly for 3 years, what was the principal amount of the loan, to the nearest dollar?
- **33**. Karen is going to invest \$1250.00. She has 2 options:

A. 7%/a compounded annually for 2 years B. 6%/a compounded monthly for 2 years Which option should she choose? Explain.

- **34**. Zachary borrowed \$3500 at a rate of 8% compounded semi-annually for 3 years. How much interest will be charged for borrowing the money?
- **35.** Solve for x: a)  $6^{3x+2} = 1$

b) 
$$5^{x^2+2x} = 125$$

**36.** The amount of a substance, A(t), left in a sample is modeled by  $A(t) = A_0 \left(\frac{1}{2}\right)^{\frac{3}{2}}$ , where t represents

the time, in weeks, after the initial time. If there are 5 mg remaining after 6 days, how much was present initially?